# Capital, Interest, and Corporate Finance 

The Role of Time In Production and Consumption Present Value and Discounting Corporate Finance

## Production, Saving, and Time

Production takes time
sannot occur without prior saving

Ex: J ones, a farmer, waiting for his crop to grow,
sa Rely on food saved from prior production
sa Could spend time to make a plow (犁)

- I ncrease his future productivity
- making the plow is time consuming


## Roundabout Production

© Making the plow $\rightarrow$ roundabout production
\& Produces capital to increase future productivity

* An increased amount of roundabout production
more capital accumulates
more goods can be produced in the future
I n modern economies,
producers need not rely exclusively on their own prior saving
ab relying on financial intermediaries for funds


## Consumption, Saving, and Time

> Most consumers value present consumption more than future consumption

a Positive rate of time preference
${ }_{3}$ Present consumption is valued more than future consumption
${ }_{3}$ Must be rewarded to postpone consumption

## Consumption, Saving, and Time

- By the saving in financial institutions,
\& Forgo present consumption
순 Consume in the future
- Interest is the reward for forgoing present consumption
- The interest rate is the annual interest as a percentage of the amount saved
- Higher the interest rate
an More rewarded for saving
${ }^{4}$ More willing to save


## Optimal Investment

- In modern economy, firms
${ }_{3}$ need not produce their own capital, ${ }^{2}$ sa need not rely upon their own saving w can purchase capital using borrowed funds
- Ex: Six pieces of farm machinery that J ones has ranked from most to least productive

See next slide

## Optimal Investment

 The payoff Table| Farm Equipment <br> (1) | Total Product (bushels) <br> (2) | Marginal Product (bushels) <br> (3) | Marginal Revenue Product $(4)=(3 \times \$ 4)$ | Marginal Resource Cost (5) |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| No equipment | 200 | - | - | - |  |
| Tractor-Tiller | 1,200 | 1,000 | \$4,000 | \$10,000 |  |
| Combine | 2,000 | 800 | 3,200 | 10,000 |  |
| Irrigator | 2,600 | 600 | 2,400 | 10,000 |  |
| Harrow | 3,000 | 400 | 1,600 | 10,000 |  |
| Crop Sprayer | 3,200 | 200 | 800 | 10,000 |  |
| Post-Hole Digger | 3,200 | 0 | 0 | 10,000 |  |

* Suppose J ones sells corn in a perfectly competitive market at \$4 per bushel
Marginal Revenue Product=Marginal Product*4
Suppose each piece of farm equipment costs $\mathbf{\$ 1 0 , 0 0 0}$


## Optimal Investment

Determine the Optimal Strategy

- Let equipment

3 is durable that it lasts indefinitely, price remain the same
a increases revenue every year into the future

## - J ones needs to find the optimal investment

## Optimal Investment

## Determine the Optimal Strategy

- J ones can't construct optimal


## strategy by

: MRC=MRP
since MRC is for this year,
sz marginal product is an annual amount for each year into the future

Markets bridge this time discrepancy with the interest rate

Optimal Investment
Compute Marginal Rate of Return
Compute the marginal rate of return on investment he would earn each year by investing in farm machinery
s marginal rate of return on investment= capital's marginal revenue product marginal resource cost

## Optimal Investment

Compute Marginal Rate of Return
For example,
ta Tractor-Tiller

- MRP: \$4,000/ year
- MRC: \$10,000
- Marginal rate of return=4000/ 10000=40\%


# The rates of return for all the farm equipment are shown in next slide 

## Optimal Investment

Table of Marginal Rate of Return on Investment

$$
\text { Marginal Rate of Return= } \frac{M R P}{M R C}
$$

| Farm Equipment <br> (1) | Total Product (bushels) (2) | Marginal Product (bushels) (3) | Marginal Revenue Product $(4)=(3 \times \$ 4)$ | Marginal Resource Cost (5) | Marginal Rate of Return $(6)=(4 / 5)$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| No equipment | 200 | - | - | - | - |
| Tractor-Tiller | 1,200 | 1,000 | \$4,000 | \$10,000 | 40\% |
| Combine | 2,000 | 800 | 3,200 | 10,000 | 32\% |
| Irrigator | 2,600 | 600 | 2,400 | 10,000 | 24\% |
| Harrow | 3,000 | 400 | 1,600 | 10,000 | 16\% |
| Crop Sprayer | 3,200 | 200 | 800 | 10,000 | 8\% |
| Post-Hole Digger | 3,200 | 0 | 0 | 10,000 | 0\% |

## Optimal Investment

## Determine the Optimal Strategy

How much should J ones invest in order to maximize profits?
Suppose he can borrow the money, at the market interest rate
a Buy more capital if

- marginal rate of return > market interest rate
Ex: market interest rate=20\%
a Invest in the first three pieces of equipment $=\$ 30,000$
Ex: I nterest rate=10\%,
\% Invest in the Harrow
Ex: Interest rate=6\%
6 I nvest in the Crop Sprayer


## Optimal Investment

Figure of Marginal Rate of Return on Investment

The data in column (6) provide the information for the step-like curve

For example, if the market interest rate is between $32 \%$ and $40 \%$,, Jones should invest in the first piece of equipment

This step-like curve $\boldsymbol{\rightarrow}$ the farmer's demand for investment.
It is a derived demand, based on equipment's marginal productivity.


## Optimal Investment

Opportunity Cost for Investing

- If J ones could save at the market interest rate
${ }_{3}$ The results would not change even if J ones used his funds
- That is, whether J ones
a borrows the money
엾 uses savings on hand,
the market interest rate represents his opportunity cost of investing


## Summary of Steps

- 1. Compute the MRP of capital

2. Compute marginal rate of return
= MRP/ MRC
s demand curve for investment

* Market interest rate= opportunity cost of investing
Firm should invest more if
sa marginal rate of return >
market interest rate


# Market for Loanable Funds <br> Demand Side 

－Major demanders of loans：
$\Leftrightarrow$ firms $\rightarrow$ borrow to invest
Firm has a variety of investment opportunities

## s Rank their opportunities based on expected marginal rates of return

${ }_{6}^{6}$ I ncrease investment until
－expected marginal rate of return＝ market interest rate
＊Households are often willing to pay extra to consume now（Ex：房貸，現金卡）约 greater willingness and ability to borrow at lower interest rates

|  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |
|  |  |  |  |  |

## Market for Loanable Funds

Banks play the role of financial intermediaries in the loanable funds market
m brings together

- savers, or suppliers of loanable funds,
- borrowers, or demanders of loanable funds, determine the market rate of interest

Higher the interest rate, other things constant,
$\because \rightarrow$ greater the reward for saving
$\Leftrightarrow \rightarrow$ the larger quantity of loanable funds

## Market for Loanable Funds

Higher interest rate $\rightarrow$ Large quantity for loanable funds


## Demand for Loanable Funds

- Diminishing marginal productivity
${ }_{x} \rightarrow$ declining marginal rate of return
$\rightarrow \rightarrow$ demand curve for investment slope downward
- The demand for loanable funds is based on the expected marginal rate of return of these borrowed funds
* The demand for loanable funds by each firm can be summed horizontally to yield the demand for loanable funds by all firms


## Market for Loanable Funds

The demand for loanable funds by all firms is shown as $D$.
Other things constant: prices of resources, the level of technology, and the tax laws.


## Market for Loanable Funds

Change in the demand or supply for loanable funds $\rightarrow$ change the market interest rate.
Ex: Technological breakthrough that increases the productivity of capital
$\rightarrow$ Demand for loanable funds shifts from $D$ to $D^{\prime}$
$\rightarrow$ Higher interest rate and an increase in the quantity of loanable funds


## Observe Interest Rate Difference:



## Observe Interest Rate Difference



## Why Interest Rates Differ

Previous arguments imply that only one interest rate prevails in the loanable funds market

## However, a range of interest rates coexist in the economy

## - Why do interest rates differ? <br> $a$ Risk $\rightarrow$ some borrowers are more likely to default

## Why Interest Rates Differ

a Duration of the loan
－Future is uncertain，
－More further into the future
$\rightarrow$ more uncertain that repayment
$\rightarrow$ Lenders require a higher interest rate
－Term structure of interest rates ：
－the relationship between the duration of the Ioan and the interest rate charge


## Why Interest Rates Differ

$a$ Cost of administration
－Costs of executing the loan agreement， monitoring the loan，and collecting the payments
－These costs，as a proportion of the total amount of the loan，decrease as the size of the loan increases（Ex：開辦費）
［1 Tax treatment
－I nterest earned on loans to local government
－Not subject to Federal tax
－Low interest rate

## Present Value and Discounting

- Present consumption is valued more than future consumption, an Can't be directly compared
* To standardizing the discussion ${ }^{5}$ a Measure all consumption in terms of its present value

> Present value (PV) is the current value of a payment(s) that will be received in the future

## Present Value One Year Hence

Suppose the market interest rate is 10\%,
a You can either lend or borrow at that rate

- To determine how much you should pay to receive $\$ 100$ one year later
연 Equivalent to how much you should save now, at the market interest rate, to get
\$100 one year from now
目 PV $1.10=\$ 100$
图 $\rightarrow P V=(\$ 100 / 1.10)=\$ 90.91$


## Present Value One Year Hence

## - Discounting:

## $\mathrm{PV}=\frac{\text { amount received one year from now }}{1+\text { interest rate }}$

${ }_{3}$ The interest rate used to discount future payments is called the discount rate
${ }^{3}$ a Note that PV depends on the interest or discount rate

- The higher the interest rate,
$\rightarrow$ the lower its PV
- The lower the interest rate,
$\rightarrow$ the greater its PV


## Present Value One Year Hence

* The more that present consumption is preferred to future consumption,
a the higher the interest rate must be offered to defer consumption
* The less present consumption is preferred to future consumption,
the less savers need to be paid to defer consumption


## PV in Later Years

Consider the PV of $\$ 100$ two years later b What amount of money, should be saved to yield $\$ 100$ two years from now?
m Let interest rate=5\%

* At the end of the first year,
: Value=PV x 1.05
* At the end of the second year,
\% See next slide


## Present Value in Later Years

Present value $\times 1.05 \times 1.05=$ present value $\times(1.05)^{\mathbf{2}}=\$ 100$

$$
\mathrm{PV}=\frac{\$ 100}{(1.05)^{2}}=\frac{\$ 100}{1.1025}=\$ 90.70
$$

A generalize equation for \$M tyears later at rate $\boldsymbol{i}$.

$$
P V=\frac{M}{(1+i)^{t}}
$$

*Remark: $(1+i)$ is greater than 1 (利率>0)
ePV of a given payment will be smaller the further into the future that payment is to be received

Present Value of an Income Stream

Most investments yield a stream of income over time
si PV of each receipt can be computed individually
5 The results summed to yield the PV of the entire income stream

## Present Value of an Annuity

－A given sum of money received each year for a specified number of years is called an annuity（年金）
－使用等比級數計算
－Such an income stream is called a perpetuity if it continues indefinitely into the future
冬 使用無窮等比級數計算

## Corporate Stock and Retained Earnings

－Corporations acquire funds for investment in three ways
sa I ssuing stock
\％Retaining some of their profits
$a$ borrowing
＊An entrepreneur
${ }^{\text {s }}$ profit－seeking decision－maker
${ }_{6}$ organizes an enterprise
\＆Pays resource owners to use their resources in the firm

Corporate Stock and Retained Earnings

6 The initial sale of stock to the public is called an initial public offering，or an I PO（初次公開發行）
＊A share of corporate stock
A claim on the net income and assets of a corporation
\％The right to vote on
－corporate directors
－important matters
：One share of stock leads to one vote

## Corporate Stock and Retained Earnings

© Corporations must pay corporate income taxes on any profit

- After-tax profit is either paid as
$a$ Dividends to shareholders
a Reinvested profit is called retained earnings and allows the firm to finance expansion
a Corporations are not required to pay dividends


## Corporate Bonds

- Corporate bond: the corporation's promise to pay back the holder a fixed sum of money (Face value)
\& on the designated maturity date
sa plus annual interest payments (coupon)
* The payment stream for bonds is more predictable than that for stocks
- Unless the corporation goes bankrupt, it is obliged to pay the promised amounts
$\rightarrow$ less risky
a Corporations are not required to pay dividends


## Securities Exchanges

＊Once stocks and bonds have been issued and sold，owners of these securities are free to resell them on security exchanges
－There are seven security exchanges in the U．S． with the two largest：
n New York Stock Exchange
s．Nasdaq
＊Secondary market for securities（次級市場）， exchanges enhance the liquidity of these securities

## Securities Exchanges

## －I nstitutional investors，such as

sa banks，
as insurance companies
an mutual funds
account for over half the trading volume on major exchanges

## The secondary markets for stocks also determine the current market value of the corporation

## Securities Exchanges

The share price reflects the PV of the discounted stream of expected profit

- Security prices give the firm's management some indication of the wisdom of raising investment funds through
ar retained earnings,
g new stock issues,
風 new bond issues


## Securities Exchanges

*The greater a corporation's expected profit, other things constant,
${ }_{3}$ higher stock price
$s$ lower the interest (coupon) rate on new bond issues

Securities markets allocate funds more readily to successful firms than to firms in financial difficulty

## 課堂報告

＊請解釋何謂roundabout production
－請解釋市場上會有不同的利率
＊請解釋在透過借貸進行投資時，如何讓投資達到最佳化
＊請說明如何計算年金（annuity）的現値
＊請說明企業有哪三種不同的集資管道

## Homework：

9．Analyze the optimal investment
10．分析市場利率的走向
－11．計算 present value

